//Modular Arithmatic

//(a+b)%m = ((a%m) + (b%m))%m

//(a\*b)%m = ((a%m) \* (b%m))%m

//(a-b)%m = ((((a%m) – (b%m)) %m)+m)%m

//to have the answer of –x % m add a big multiple value of m (suppose y) with –x, so that it becomes (y-x) positive

//then modulo that number

inline ull odd(ull n) {

return (n & 1); //returns true if n is odd faster than n%2

}

inline ull powmod(ull n, ull p, ull m) {

if(p == 0) return 1;

if(!odd(p)) {

ull tmp = powmod(n, p/2, m)%m;

return (tmp\*tmp)%m;

}

else return ((n%m)\*(powmod(n, p-1, m)%m))%m;

}

inline ull plusmod(ull x, ull y, ull m) {

return ((x%m)+(y%m))%m;

}

long long Power(long long x, long long y) {

if(y == 0) return 1;

if(y&1) return x\*Power(x\*x, y/2);

else return Power(x\*x, y/2);

}

//Extended Euclid

//ax + by = c can be solved if d = gcd(a, b) and d | c (d divides c, or d is multiple of c), there may be infinite number of //solutions (x <= y), these can be generated by, x = x1 + (b/d)n & y = y1 – (a/d)n

//x1 = x \* (c/d), y1 = y \* (c/d)

//lower = ceil((-x1\*d)/b), upper = floor((y1\*d)/a) , ans exists only if lower <= upper

//lower and upper both can be negative or positive

//here a, b, x, y, n all are integers

//declare x, y, z globally

void extendedEuclid(ll a, ll b) {

if(b == 0) {x = 1; y = 0; d = a; return;}

extendedEuclid(b, a%b);

int x1 = y;

int y1 = x - (a/b) \* y;

x = x1;

y = y1; }

//Prime Generator and factorization

bitset<N>bit;

vector<ll> factors, prime;

ll power[N];

void sieve() {

bit.set();

bit[0] = bit[1] = 0;

for(ll i = 0; i <= N; i++) { //it can be limited to sqrt(N)

if(bit[i]) { //here it is not used as we want to0

for(ll j = i \* i; j <= N; j += i) //save the primes in prime vector

bit[j] = 0;

prime.pb(i);

} } }

void primeFactor\_of\_factorial(ll n) { //n!

memset(power, 0, sizeof(power));

for(size\_t i = 0; prime[i] <= n && i < prime.size(); i++) {

int tmp = n;

wh(tmp) {

power[prime[i]] += tmp / prime[i]; //if we want to generate powers and numbers

//factors.pb(prime[i]); //if we only to genetare all the numbers

tmp /= prime[i];

} } }

void primeFactor(ll n) {

memset(power, 0, sizeof(power));

if(prime[n]) { //First determine if n is a prime number

power[n]++;

//factors.pb(n);

}

else {

for(size\_t i = 0; prime[i]\*prime[i] <= n && i < prime.size(); i++) {

wh(n % prime[i] == 0) {

power[prime[i]]++;

//factors.pb(prime[i]);

n/=prime[i];

} }

if(n > 1) { //Must be a prime number which is not in prime[i]

power[n]++; //it would happen if n is a large number

//factors.pb(n);

} }

//Math formulas

//Subsets (2^n)

int main() {

int len, s = 0, sub\_sum\_find, tmp, subset\_sum[10000];

scanf(" %d", &len);

int arr[len+1]; //arr is containing the numbers

for(register int i = 0; i < len; i++)

scanf(" %d", &arr[i]);

scanf("%d", &sub\_sum\_find);

for(register int i = 0; i < (1 << len); i++) {

subset\_sum[s] = 0;

for(register int j = 0; j < len; j++)

if(i & (1 << j)) //this point can be noted by saving i

subset\_sum[s] += arr[j];

if(subset\_sum[s] == sub\_sum\_find) tmp = i;

s++;

}

for(register int j = 0; j < len; j++)

if(tmp & (1 << j))

printf("%d ", arr[j]); //generates the numbers

return 0;

}

//2D Max Sum

int main() {

register int n, i, j, k, l, maxsubrect, subrect;

int A[110][110];

while(scanf(" %d", &n) != EOF) {

for(i = 0; i < n; i++)

for(j = 0; j < n; j++) {

scanf(" %d", &A[i][j]);

if(i > 0) A[i][j] += A[i-1][j];

if(j > 0) A[i][j] += A[i][j-1];

if(i > 0 && j > 0) A[i][j] -= A[i-1][j-1];

}

maxsubrect = -127\*100\*100;

for(i = 0; i < n; i++)

for(j = 0; j < n; j++)

for(k = i; k < n; k++)

for(l = j; l < n; l++) {

subrect = A[k][l];

if(i > 0) subrect -= A[i-1][l];

if(j > 0) subrect -= A[k][j-1];

if(i > 0 && j > 0) subrect += A[i-1][j-1];

maxsubrect = max(maxsubrect, subrect);

}

printf("2D Max Sum: %d\n", maxsubrect);

}

return 0;

}

//1D Max Sum

sum = mx = 0;

for(int i = 0; i < n; i++) {

sum += a[i]; //a[i] contains the numbers

if(sum < 0) sum = 0;

else if(sum > mx) mx = sum;

}

pf("1D Max Sum: %lld\n", mx);

//Coin Change (DP)

// n is the amount we need to produce

// coin[] array contains the coins we can use

int coin[] = {1, 2, 3}, test[1000];

int main() {

while(1) {

int n, coin\_amount = 3;

scanf("%d", &n);

// Solution for producing amount with coins. Without any co-occurance and

// coins can be used more than once

// Bottom Up solution

memset(test, 0, sizeof(test));

test[0] = 1; // Base case

for(register int i = 0; i < coin\_amount; i++) // this will NOT produce co-occurance

for(register int j = 1; j<=n; j++) // solution for 4 if there is present 1 & 2 coins would be 3

if(j >= coin[i]) // 1+1+2, 2+2, 1+1+1+1

test[j] += test[j - coin[i]];

printf("Solution without co-occurance : %d\n", test[n]);

// Solution for producing amount with coins. With co-occurance and

// coins can be used more than once

// Bottom Up solution

memset(test, 0, sizeof(test));

test[0] = 1; // Base case

for(register int j = 1; j <= n; j++) // this will produce co-occurance

for(register int i = 0; i < coin\_amount; i++) // solution for 4 if there is present 1 & 2 coins would be 5

if(j >= coin[i]) // 1+1+2, 2+2, 1+1+1+1

test[j] += test[j - coin[i]]; // and also 2+1+1, 1+2+1

printf("Solution with co-occurance : %d\n", test[n]);

// Solution for producing amount with coins. With co-occurance and

// coins can be used more than once

// Top Down solution

memset(test, inf, sizeof(test));

test[0] = 0; // Base case

for(register int i = 0; i < coin\_amount; i++) // this will produce co-occurance

for(register int j = n; j > 0; j--) // solution for 4 if there is present 1, 2 & 3 coins would be 2

if(j >= coin[i] && (test[j - coin[i]] + 1) < inf) // 1+3, and 3+1

test[j] = test[j-coin[i]] + 1;

printf("Solution by using coins only once with co-occurance : %d\n", test[n]);

}

return 0;

}

//Data Structure

//Segment Tree

int arr[N], tree[4\*N]; //Always take the tree 4 times bigger

void segment\_build(int pos, int L, int R) {

tree[pos] = 0;

if(L==R) {

tree[pos] = arr[L];

return;

}

int mid = (L+R)/2;

segment\_build(pos\*2, L, mid);

segment\_build(pos\*2+1, mid+1, R);

tree[pos] = tree[pos\*2] \* tree[pos\*2+1];

}

void segment\_update(int pos, int L, int R, int i, int val) {

if(L==R) {

tree[pos] = val;

return;

}

int mid = (L+R)/2;

if(i <= mid)

segment\_update(pos\*2, L, mid, i, val);

else

segment\_update(pos\*2+1, mid+1, R, i, val);

tree[pos] = tree[pos\*2] \* tree[pos\*2+1];

}

int segment\_query(int pos, int L, int R, int l, int r) {

if(R < l || r < L) return 1;

if(l <= L && R <= r) return tree[pos];

int mid = (L+R)/2;

int x = segment\_query(pos\*2, L, mid, l, r);

int y = segment\_query(pos\*2+1, mid+1, R, l, r);

return x\*y;

}

//Data Structure

//Union Disjoint Set

ll u\_set[N+100], u\_list[N+100];

//u\_set is used to determine set

//u\_list is used to keep track of the nodes that each node connects (as a root)

inline ll root(ll n) { //finding the root of a set

if(u\_set[n] == n)

return n;

else

return u\_set[n] = root(u\_set[n]); //path compression

}

inline ll make\_union(ll a, ll b) { //make union of set, returns the value of

ll x = root(a); //the new root

ll y = root(b);

if(x == y) //returns the same value if the input two

return x; //value is same

else if(u\_list[x] > u\_list[y]) {

u\_set[y] = x;

u\_list[x] += u\_list[y];

return x;

}

else {

u\_set[x] = y;

u\_list[y] += u\_list[x];

return y;

} }

void union\_init(ll l) { //initialising of set and list

for(ll i = 0; i <= l; i++) {

u\_list[i] = 1;

u\_set[i] = i;

} }

//Graph Theory

//BFS

//Shortest Path in unweighted graph

//the level from a node u is the shortest path from u to any node in unweighted graph

//scans in a layer way

void bfs(int u) {

queue<int>q; //parent[v] = u

visited[u] = 1;

level[u] = 0;

parent[u] = -1; //the source's parent is tagged

q.push(u); //pushing the starting node in queue

wh(!q.empty()) {

int U = q.front();

q.pop();

for(size\_t i = 0; i < g[U].size(); i++) { //using adjency list g[node]

int v = g[U][i];

if(!visited[v]) {

level[v] += level[u]+1; //saving the distance

past[v] = U; //the parent nodes are saved

visited[v] = 1; //visited nodes are tagged

q.push(v); //visited nodes are pushed for next //iteration

}}}}

//in main functio

for(int i = 0; i < node; i++) if(!visited[i]) bfs(i); //check every connected/non connected node

memset(visited, 0, sizeof(visited)); //to track the nodes which are visited

memset(parent, 0, sizeof(parent)); //to track the parent nodes

//BFS Bipartite

//if the graph cycle is odd then it is not bi-colorable

bool bipartite(int u) {

queue<int>q;

q.push(u);

color[u] = 0; //color must be memset to inf in main func.

isBipartite = true; //tag to check if its bipartite

while(!q.empty()) {

int U = q.top();

q.pop();

for(size\_t i = 0; i < g[U].size(); i++) {

int v = g[u][i];

if (color[v] == INF) { //instead of recording distance,

color[v] = 1 - color[u]; //just record two colors {0, 1}

q.push(v);

}

else if (color[v.first] == color[u]) { // u & v has same color

isBipartite = false;

break; //we have a coloring conflict

} } }

//DFS

//basic implimentation

//check if node v is visitable from u. if so, dfs\_num[v] == 1

//scans each sub nodes till the end first

void dfs(int u) {

dfs\_num[u] = 1; //dfs\_num zero initialized in main(), set counter to 1

for (size\_t i = 0; i < g[u].size(); i++) { // Adjency list

int v = g[u][j]; // v is the visitable node from node u (u -> v)

if (dfs\_num[v] == 0) // important check to avoid cycle, its not visited

dfs(v); // recursively visits unvisited neighbors of vertex u

} }

//Flood Fill

//Size of connected component

int dr[] = {-1, -1, -1, 0, 0, 1, 1, 1};

int dc[] = {-1, 0, +1, -1, +1, -1, 0, +1}; // trick to explore an implicit 2D grid

int floodfill(int r, int c) {

if(r < 0 || r >= R || c < 0 || c >= C) return 0; //checking the bounderies

if(g[r][c] != tag || visited[g[r][c]]) return 0; //checking if the grid is valid

cc\_size++; //increasing connected component size

visited[g[r][c]] = 1;

for(int i = 0; i < 8; i++)

floodfill(r + dr[i], c + dc[i]); //recursion to all other side grids

}

//Topological Sort

//Directed Acyclic Graph (DAG)

//dfs\_num[x] = number of dfs done in dfs\_num, (visited or not instead)

//in topological sort all nodes are linierly sorted in a way that all nodes point to the same //direction (to left or right)

void topology(int u)

{

dfs\_num[u] = 1;

for(size\_t i = 0; i < g[u].size(); i++)

if(dfs\_num[g[u][i]] == 0)

dfs2(g[u][i]);

topsort.push(u); //its a stack sorted from first to last

}

//DFS spanning tree / forest

//UNVISITED -> 0

//EXPLORED -> 1

//VISITED -> 2

//tree edge (sub tree)

//back edge (cycle)

//forward edge (cross edge)

void dfstree(int u) {

dfs\_num[u] = 1;

for(size\_t i = 0; i < g[u].size(); i++) {

int v = g[u][i];

if(dfs\_num[v] == 0) { //if the node is unvisited, tree edge

dfs\_parent[v] = u; //the parent of v is u

graphCheck(v);

}

else if(dfs\_num[v] == 1) { //if the node is explored, but full dfs not done

if(dfs\_parent[u] == v) //if the node's parent is its child node (Undirected)

pf("Two ways (%d %d)-(%d %d)\n", u, v, v, u);

else //only option is left is backedge

pf("Back Edge (%d %d) (Cycle)\n", u, v);

}

else if(dfs\_num[v] == 2) //it the child node's dfs is done, its a forward edge

pf("Forward/Cross Edge (%d %d)\n", u, v);

}

dfs\_num[u] = 2; //in this point the full dfs is done

}

//Articulation Point and Bridge

//Bridge : An edge is a bridge if and only if it is not contained in any cycle

//Articulation Point: A node is articulation point if disconnecting it creates

//more connected component (cc)

//dfs\_num[x] = n : the n'th number dfs done in node x

//dfs\_low[x] = n : the minimum dfs\_num in node x from its sub tree and back-edge

//without considering node x

void ArticulationPointandBrdge(int u) {

dfs\_low[u] = dfs\_num[u] = dfsNumberCounter++; //at first all are same

for(size\_t i = 0; i < AdjList[u].size(); i++) {

int v = AdjList[u][i];

if(dfs\_num[v] == 0) { //tree edge (subtree) unvisited condition

dfs\_parent[v] = u; //memorising the parent node

if(u == dfsRoot) rootChildren++; //special case if u is root

ArticulationPointandBrdge(v); //visiting the next node before checking

if(dfs\_low[v] >= dfs\_num[u]) //this denotes that it has sub tree or back-edge

articulation\_vertex[u] = true; //articulation vertex found

if(dfs\_low[v] > dfs\_num[u]) //this denotes that it has no back-edge

pf("Edge (%d, %d) is a bridge\n", u, v); //bridge found

dfs\_low[u] = min(dfs\_low[u], dfs\_low[v]); //dfs\_low is the minimum dfs\_num

} //of its sub tree

else if(v != dfs\_parent[u]) //a back edge (not a direct cycle)

dfs\_low[u] = min(dfs\_low[u], dfs\_num[v]); //checking the back edge dfs\_num

}}

//Strongly Connected Components (Directed Graph)

//only works in directed graph tarjan's algorithm (dfs implement)

vector<int> S;

bool visited[node];

void tarjanSCC(int u) {

dfs\_low[u] = dfs\_num[u] = dfsNumberCounter++; // dfs\_low[u] <= dfs\_num[u]

S.push\_back(u); // stores u in a vector based on

visited[u] = 1; //order of visitation

for (int j = 0; j < (int)g[u].size(); j++) {

v = g[u][j];

if (dfs\_num[v] == 0)

tarjanSCC(v);

if (visited[v]) // condition for update

dfs\_low[u] = min(dfs\_low[u], dfs\_low[v]);

}

if (dfs\_low[u] == dfs\_num[u]) { // if this is a root (start) of an SCC

printf("SCC %d:", ++numSCC); // this part is done after recursion

while (1) { //group of scc is generated here

int v = S.back(); S.pop\_back(); visited[v] = 0;

printf(" %d", v); //v is a node of this scc

if (u == v) break; //breaks if it is the last component

} } }

// inside int main()

//dfs\_num, dfs\_low, visited are assigned to 0

dfsNumberCounter = 0;

for (int i = 0; i < V; i++)

if (dfs\_num[i] == UNVISITED) //don't depend on visited, cause it is for the algo

tarjanSCC(i);

//Dikjstra’s Algorithom Shortest Path

//Only works if cost is positive

//use dikjstra(u) if shortest path from u to other nodes are needed to be found

void dikjstra(int u)

{

fr(i, 0, arrsize(dis)) dis[i] = inf; //dis[node] = distance

priority\_queue<pii>pq; //priority queue to sort the nodes according their cost

dis[u] = 0; //setting starting distance to zero

pq.push(mp(u, dis[u])); //node, distance

while(!pq.empty()) { //cost[u][v] = cost of u -> v

u = pq.top().first; //taking the smallest node of shortest distance

pq.pop();

for(size\_t i = 0; i < g[u].size(); i++) {

int v = g[u][i];

if(dis[u] + cost[u][i] < dis[v]) {

dis[v] = cost[u][i] + dis[u];

pq.push(mp(v, dis[v]));

} } } }

//Bellman Ford Algo

//Can be used when a graph has negative cost and cycle (negative cycle)

//complexity for adjency list O(v^2)

//the code runs v-1 times for all nodes

void bellmanFord(int U) {

fr(i, 0, V+1) dist[i] = inf;

dist[U] = 0; //setting start node to zero

for(int i = 0; i < V -1; i++) //this loop runs V-1 times

for(int u = 0; u < V; u++) //each time for all nodes

for(size\_t j = 0; j < g[u].size(); j++) {

int v = g[u][j];

dist[v] = min(dist[v], dist[u] + cost[u][j]);

} }

//to check if a graph has negative cycle on it, first run bellmanford, then run this

bool negativeCycle() {

bool hasNegativeCycle = 0;

for(int u = 0; u < V; u++)

for(size\_t j = 0; j < g[u].size(); j++) {

int v = g[u][j];

if(dist[v] > dist[u] + cost[u][j]) { //the main case

hasNegativeCycle = 1; //to check

break; }}

return hasNegativeCycle;

}

//Bitwise Operations and Tricks

Is n’th bit set : x & (1 << n) == 1

Set the n’th bit : x |= (1 << n)

Unset/reset n’th bit : x &= ~(1 << n)

Toggle n’th bit: x ^= (1 << n)

Turn off rightmost bit(if it is on): x & (x - 1)

Isolate the rightmost 1 bit: x & (-x) //only remains the rightmost bit

Right propagate the rightmost 1 bit : x | (x-1) //10100 becomes 10011

Isolate rightmost 0 bit : ~x & (x+1)

Turn on rightmost 0 bit : x | (x+1)

Turn all bits from right : (1 << n) – 1; //(1 << 7) – 1 = 1000000 – 1 = 111111

Some usage ::

Patterns -> 100100 – 1 = 100011, 10000 – 1 = 1111

Test if two bitsets coincide atleast at one point : bit1 & bit2

To add two bitsets on state : bit1 | bit2

Find mismatches of bit1 and bit2 : bit1 ^ bit2

Elaminate mismatch from bit1 and bit2 : bit1 & bit2

To check if bit1 contains some bits (or not) which are turned off in bit 2 or same bits turned on: ((bit1 ^ bit2) & bit2) //nonzero on true

//Topological Sort

//Khan’s Algorithm

//Complexity : O(V+E)

void topsort()

{

int indegree[110];

memset(indegree, 0, sizeof(indegree));

for(int i = 0; i <node.size(); i++)

for(int i = 0; i < G[node[i]].size(); i++)

indegree[G[node][i]]++;

priority\_queue<int, vector<int>, greater<int> >pq; //Normally queue can be used

//priority queue is used to avoid special formating cases

for(int i = node.size()-1; i >= 0; i--)

if(indegree[node[i]] == 0)

pq.push(node);

//int cnt = 0; //to detect if the graph is Acyclic, check below

vector<int>ans;

while(!pq.empty()) {

int u = pq.top();

pq.pop();

ans.push\_back(u);

for(int i = 0; i < G[u].size(); i++)

if(--indegree[G[u][i]] == 0)

pq.push(G[u][i]);

//cnt++;

}

//if(cnt != to\_int.size()) //it has no topological order (Acyclic)

//ans vector contains the topological order

}

//Trie, Radix Tree

struct node {

bool endmark;

node\* next[26 + 1];

node()

{

endmark = false;

for (int i = 0; i < 26; i++)

next[i] = NULL;

}

} \* root;

void insert(char str[], int len)

{

node\* curr = root;

for (int i = 0; i < len; i++) {

int id = str[i] - 'a';

if (curr->next[id] == NULL)

curr->next[id] = new node();

curr = curr->next[id];

}

curr->endmark = true;

}

bool search(char str[], int len)

{

node\* curr = root;

for (int i = 0; i < len; i++) {

int id = str[i] - 'a';

if (curr->next[id] == NULL)

return false;

curr = curr->next[id];

}

return curr->endmark;

}

void del(node\* cur)

{

for (int i = 0; i < 26; i++)

if (cur->next[i])

del(cur->next[i]);

delete (cur);

}

//in case of getting input as suffixes, use this

//NOTE : substrings are prefix of suffixes

for(int i = 0; i < len; i++)

insert(input\_str+i, len-i);

//KMP String Matching

//Complexity 0(T+P)

// T = text, P = pattern

int P\_Size, T\_Size, Table[1000010];

void PrefixTable()

{

register int i = 0, j = -1;

Table[0] = -1;

while(i < T\_Size) {

while(j >= 0 && T[i] != T[j])

j = Table[j];

i++, j++;

Table[i] = j;

}

}

int KmpSearch()

{

register int i = 0, j = 0, cnt = 0;

while(i < P\_Size) {

while(j >= 0 && P[i] != T[j])

j = Table[j];

i++, j++;

if(j == T\_Size) {

cnt++; //the match found in i-j

//printf("%d'th Match found at %d\n", cnt, i-j);

j = Table[j];

}

}

return cnt;

}

//Longest Common Subsequence of two string

//Dynamic Programming

//a = string 1, b = string 2;

char a[210], b[210];

int dp[210][210], len\_a, len\_b;

int LCS()

{

for(register int i = 1; i <= len\_a; i++)

for(register int j = 1; j <= len\_b; j++) {

if(i == 0 || j == 0) //base case

dp[i][j] = 0;

else if(a[i-1] == b[j-1]) //if a match found

dp[i][j] = dp[i-1][j-1] + 1;

else

dp[i][j] = max(dp[i-1][j], dp[i][j-1]);

// dp[i][j] = max(ignoring b[j-1] (taking b[j]), ignoring a[i-1] (taking a[i]))

}

return dp[len\_a][len\_b];

}

void printLCS()

{

// Create a character array to store the lcs string

int index = dp[len\_a][len\_b];

char lcs[index+1];

lcs[index] = '\0'; // Set the terminating character

// Start from the right-most-bottom-most corner and

// one by one store characters in lcs[]

int i = len\_a, j = len\_b;

while (i > 0 && j > 0) {

// If current character in X[] and Y are same, then

// current character is part of LCS

if (a[i-1] == b[j-1]) {

lcs[index-1] = X[i-1]; // Put current character in result

i--; j--; index--; // reduce values of i, j and index

}

// If not same, then find the larger of two and

// go in the direction of larger value

else if (dp[i-1][j] > dp[i][j-1])

i--;

else

j--;

}

// Print the lcs

cout << "LCS of " << X << " and " << Y << " is " << lcs;

}